

MATHEMATICAL THEOREM UTILITY IN DEEP LEARNING PROCESS

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Abstract

This work investigates the ways in which logical deductions in deep learning and automated theorem proving (ATP) are enhanced by mathematical theorems. We start by going over the development of AI research in the field of theorem proving and how computers have altered the field, particularly in applied mathematics. Theorem-proving computers of today perform well in large-scale case analysis but fall short in complex reasoning and practicality. We then go over the ability of machine learning algorithms to automatically identify complex patterns in datasets for prediction and inference. We stress that in order to identify and reduce bias, strong and representative datasets are essential before utilising machine learning approaches. We also review studies on machine learning and mathematical modelling in arrhythmia susceptibility prediction, COVID-19 forecasting, and hepatitis C virus dynamics. These projects show how machine learning and mathematical modelling may produce precise forecasts and resolve challenging problems.

Keywords: *Automated theorem proving, Machine learning, Deep learning, Mathematical modeling, Pattern recognition, Artificial intelligence*

1. INTRODUCTION

The regular objective of AI research was to demonstrate mathematical theorems. In any case, after early triumphs, trust blurred, as the AI theorem demonstrated. This doesn't reduce the worth of PC aided confirmations of theorems and other PC based mathematical applications. In applied science, PCs are fundamental. However mathematical theorem confirmation will be the main accentuation of this review, this is a significant point. Through the headway of PC helped theorem proving in late many years, PCs can affect science. Various theorems, for example, the Kepler guess and the four-variety theorem, have been exhibited by PCs. Theorem-proving PCs these days, be that as it may, are restricted in what they can do, subsequently their verifications are not equivalent to those of human mathematicians.

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Utilizing savage power calculation, current PC confirmations exhaust a limited number of models consistently.

Programming aids in the confirmation of theorems and sensible thinking. In automated theorem proving (ATP), confirmation right hand programming can be utilized to audit existing evidences and produce new verifications and theorems. Utilizing particular calculations, a normal automated theorem proving program addresses consistent math surmisings. Rule-based programming has various benefits. We can depend on them as we know about their calculation. Automated theorem provers in view of rules have limits. Despite the fact that their mechanical strategy functions admirably, they don't care a whole lot about the verification or the theorem. All in all, despite the fact that they are alluded to as AI applications, they are not intelligent.

2. MACHINE LEARNING APPROACHES

Complex patterns in a dataset can be consequently recognized for surmising or expectation in new datasets through machine learning⁵. Uniform info gatherings can be recognized utilizing machine learning (solo learning). At the point when each occurrence has a gathering or classification mark, machine learning procedures can fabricate a classifier or relapse capability to foresee the enrollment of approaching cases in a given class (directed learning). To improve machine learning execution in a dataset, all expected wellsprings of predisposition ought to be recognized, eliminated, or diminished to a base. Representativeness thusly needs to precede machine learning.

3. LITERATURE REVIEW

Churkin et al. (2022), Hepatitis C infection (HCV) elements mathematical models have given a method for surveying antiviral medication viability and anticipate treatment results, for example, time to fix. The main evidence of-idea clinical preliminary assessing the viability of reaction directed therapy with direct-acting antivirals (DAAs) progressively for patients with constant HCV contamination as of late utilized a mathematical demonstrating approach. Various review studies have shown that in many patients treated with sofosbuvir-based regimens as well as other DAA regimens, mathematical demonstrating of viral elements predicts a chance to fix of under 12 weeks. To empower ongoing displaying research, an information base of these investigations was made, and machine learning

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procedures were assessed for their ability to foresee every patient's chance to recovery. Information were assembled from these examinations that took a gander at 266 persistently HCV-contaminated individuals' HCV energy under DAAs utilizing mathematical displaying. To gauge an opportunity to fix on the untrained segment (alluded to as the "test" set), a few learning calculations were executed and trained on a piece of the dataset (alluded to as the "train" set). Our discoveries infer that our machine learning technique offers a method for giving an exact opportunity to fix gauge, which will permit modified treatment to be carried out.

Wilmott (2022), Each innovative discipline, including machine learning (ML), has its own dialect. Finding normal movements in information can be achieved using head parts examination. One normal technique for assessing boundaries in a factual/probabilistic model is most extreme probability assessment. A straightforward strategy for evaluating a calculation's exhibition in ordering inputs is to check out at its disarray grid. How much a mathematical model digresses from the real information is communicated in machine learning (ML) utilizing an expense capability or misfortune capability. To limit the expense capability, one adjusts the mathematical model, typically by changing model boundaries. For NLP, a few of the essayists' methods are applied. Text and discourse are seen, deciphered, answered, and sorted utilizing NLP calculations.

Masum et al. (2022), 1,209,505 Coronavirus passings and 47,209,305 cases had been enrolled around the world as of November 2, 2020. Understanding the elements of the infection and extending the quantity of affirmed cases are essential for measuring the spread of a flare-up and creating approaches for the utilization of clinical assets and viral control. This work utilized a measurable model, RNN varieties, and a mathematical pestilence model (MEM) to foresee combined affirmed cases. They fostered a repeatable structure for stochastic RNN variations utilizing z-score exception distinguishing proof. Weakness heterogeneity, lockdowns, and the unique reliance of transmission and recognizable not set in stone by Poisson probability fitting were undeniably considered in the MEM. Albeit the MEM offered extensive bits of knowledge into infection spread and control strategies, the testing discoveries showed that RNN variations estimated all the more precisely.

Pavlyutin et al. (2022), The fundamental upsides of spread markers have been laid out to conjecture the spread of Coronavirus and illuminate Moscow's dynamic on prohibitive

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measures. To decide the expectation exactness and the restrictions of mathematical strategies for foreseeing disease spread for longer than two weeks, a model was made using standard outstanding relapse techniques. To increment long haul gauge exactness for over two weeks, two machine learning models are proposed: a 1-D convolutional brain network with a streamlining calculation portrayal, and a repetitive brain network with two layers of long transient memory (LSTM) blocks. For figure precision, ML models were contrasted with outstanding relapse models utilizing information from the Moscow Coronavirus contextual analysis.

4. DEEP LEARNING MODELS

- **Neural Network Architecture**

To model a deep neural network, use functions to represent linked layers. Let signify the network's total layers and represent its layers. Neurons make up each layer. Layer weights and biases are and.

- **Activation**

Complex pattern learning is made conceivable by enactment capabilities, which give the organization nonlinearities. GELU, ReLU, and exaggerated digression (tanh) actuation capabilities are every now and again utilized. Remember that the GELU capability displayed beneath is just a guess, given by the situation:

$$\text{ReLU}(x) = \max(0, x),$$

$$\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}},$$

$$\text{GELU}(x) = 0.5x \left(1 + \tanh \left(\sqrt{\frac{2}{\pi}} (x + 0.044715x^3) \right) \right).$$

- **Loss Function and Optimization**

To improve the brain organization, a misfortune capability that assesses the disparity among expected and genuine result is required. The occupation decides the misfortune capability to utilize. The normal relapse misfortune capabilities incorporate MSE, MAE, and Huber misfortune.

$$\begin{aligned} \text{MSE}(y, \hat{y}) &= \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2, \\ \text{MAE}(y, \hat{y}) &= \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|, \\ \text{Huber}(y, \hat{y}) &= \frac{1}{n} \sum_{i=1}^n \begin{cases} \frac{1}{2} (y_i - \hat{y}_i)^2, & \text{if } |y_i - \hat{y}_i| \leq \delta, \\ \delta \left(|y_i - \hat{y}_i| - \frac{1}{2} \delta \right), & \text{otherwise,} \end{cases} \end{aligned} \quad (4)$$

5. CONCLUSION

This work has highlighted the role that mathematical theorems play in improving the deep learning process. This is particularly valid when considering logical deductions and automated theorem proving (ATP). The technique of proving theorems in applied mathematics has been revolutionized by computers, yet modern ATP systems still fall short of the level of nuanced reasoning possessed by human mathematicians. However, by fusing mathematical ideas with machine learning applications, such as pattern recognition and inference, we can raise the effectiveness and efficiency of ATP systems.

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